"Smartphone-based GNSS Positioning – Today and Tomorrow"

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Keywords :

1. Introduction

The vast majority of GNSS receivers today are installed in Smartphones with 1.5 billion devices produced every year (GSA 2019). Most of these newly produced phones make GNSS raw measurements available to the applications, a feature supported by the Android operation system since 2017. This led to numerous new Smartphone applications and 1000+ research papers focusing on GNSS positioning with Smartphones (Van Diggelen et al. 2020).

An increasing number of these phones is supporting dual frequency measurements on the L1 and L5 bands. The use of an additional frequency (L5/E5a) with higher chipping rate (10 times to that of L1) results in a narrower correlation peak, making the measurements more precise and eliminating some of the multipath distortions. While these developments pave the way to transfer high precision positioning technology from expensive professional devices to mass-market Smartphones, there is still the major hurdle of successful carrier phase positioning (i.e. ambiguity fixing) to overcome before reliable dm or cm level positioning is achieved with phones.

In this article we review some of the recent results analyzing the feasibility of carrier-phase based positioning with Smartphone data and highlighting limitations largely arising due to the poor antenna quality. We also show how they might be overcome e.g. by antenna calibration or coupling to the inertial sensors inside the phone.

2. Towards cm-level Positioning

To assess the suitability of the Smartphone observations for cm-level positioning, the quality of the measurements needs to be investigated. Processing tools like (RTKLIB, 2013), (Inertial Explorer, 2021) or GNSMART, 2021) can be used for this task. To provide these tools sensor data from the Smartphones, a logger is needed. This requirement leads to the development of an Android based logger applications that log GNSS measurements and inertial sensor data which can be processed with wide variety of processing tools available in the market. The unified goal of the research work discussed in the paper is to perform a successful RTK positioning with the Smartphone quality data. The data logging and analysis was performed using the range of Smartphones. Their nomenclatures mentioned in the section 6 are used throughout the paper.

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2.1. GNSS Data Logging

Until API Level 23 (Android 6 Marshmallow) it was only possible for the applications developers to access the already estimated GNSS position and processed almanac. But with the new classes GnssMeasurements (the actual measurements of the signals of the built-in GNSS Chips), GnssNavigationMessage (the bit-wise breakdown of the navigation message) and GnssClock (the clock parameters of the receiver) that were introduced in API Level 24, more advanced data is now available via the Android Location API.

The Geo++ RINEX Logger application was the first application that converted the raw observables from the Android API directly into RINEX files that could be used in established GNSS processing frameworks. It has been optimized with the feedbacks from over a hundred users and now generates meaningful data for a large amount of Smartphone models. It has been downloaded more than 10000 times and is the most widely used logging application for GNSS raw data from phones.

The GNSS/IMU logger app developed at the Institute of Space Research and Space Applications (ISTA-UniBwM), is an extension of the Google logger and exploits the full potential of the APIs available by enabling the user to log GNSS Raw Measurements, GNSS RINEX observation and additionally IMU data (Accelerometer and Gyroscope) from the Smartphone. Additionally, the application has introduced real time Code minus Carrier (CMC) plots to visualize the carrier-phase tracking capability of the Smartphone (Figure 1).



Figure 1: Geo++ Logger (Left) GNSS/IMU Logger User Interface (Right)

Other parties have developed logging applications and Table 1 gives an overview of most used such applications.

Android App	Current Version	Developer	RINEX	Raw data	IMU
Geo++ RINEX Logger (Geo++, 2020)	2.1.6	Geo++ GmbH	yes	-	-
GNSS/IMU Logger (UniBwM, 2020)	v1.0.0.1	ISTA- UniBwM	yes	yes	yes
GNSS Logger (Google,.2021)	v3.0.0.0	Google Inc.	yes	yes	yes
rinex ON (Nottingham, 2019)	1.3	Nottingham Scientific Ltd	yes	-	-

Table	1	÷	List	of	GNSS	Data	loaaer
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In addition to these four presented applications in Table 1, there are 200+ applications on the Google Play Store capable of logging GNSS (and partly raw) data. This shows the large and growing interest in this area. Potential applications for precise positioning in Smartphones include e.g.: augmented reality, gaming, and location-based services.

2.2. Raw GNSS Measurement Analysis

The availability of raw GNSS measurements from the Smartphone does not guarantee the feasibility of successful RTK positioning. Due to limited access to the GNSS chip hardware, it is difficult to evaluate the baseband processing performance of the GNSS chip. Instead, we can only analyze the observation data of the Smartphone. To overcome this limitation, we try to emulate a Smartphone like scenario inside the MuSNAT GNSS Software-Receiver. MuSNAT developed at UniBwM, is a real-time/post-processing tool capable of performing GNSS/IMU data processing. The concept to emulate the Smartphone measurements is to introduce artifacts (code noise, carrier noise, gaps and cycle slips) in high quality IF samples (logged with SX3 front-end) and to match the quality of this corrupted data, to the observation data collected from the Smartphone (Sharma et al. 2019). The data logging procedure is explained in the Figure 2.



Figure 2: Retransmission Setup for logging IF Samples using Front-End

The IF samples recorded with SX3 front-end can be processed with the MuSNAT where the mentioned artefacts are added before being passed to the navigation module. Different scenarios generated with logged IF samples and device 2 (discussed in Table 2) were processed with the RTKLIB module inside the MuSNAT (Figure 3).

Scenario	Description of resulting RINEX data
Scenario 0	Re-transmission setup data collected with device 2 (Smartphone)
Scenario 1	High quality data collected using SX3 frontend and processed with MuSNAT
Scenario 2	Scenario 1 but random noise was added to code and carrier on the satellite G17 of the data collected using SX3 (Scenario 1)
Scenario 3	Scenario 2 plus few cycle slips were introduced on satellite G08 and G17 and several cycle slips were induced on every epoch of satellite G23, G28 and G31

Table 2: List of different scenarios emulated

On analyzing the code and the carrier residual with the induced artifacts in the IF samples, we were able to achieve similar performance parameters with the Smartphone emulation within MuSNAT as measured by device 2. The analysis shows the significance of noise present in the code and carrier measurements and their impact on the positioning performance as seen in Figure 4. The residuals between the measured and predicted code or carrier pseudoranges, contain the receiver position error and clock offsets, plus miss-modelling and measurement noise errors. These analyses can thus be helpful to achieve better decorrelation of errors induced due to the miss-modelling.







Figure 3: RINEX data set used to achieve Smartphone emulation within MuSNAT. A red solid line indicates a cycle slip







Figure 4: Code and Carrier Analysis (Top), Positioning Result (bottom) for the different scenarios

The similar retransmission setup (see Figure 2) of Scenario 0 was then extended to other Smartphones available in the market. This makes it possible to compare the average code and carrier residual for different Smartphones. These results presented in Figure 5 (also summarized Table 3), indicates that the device 3 provides a better combination of code and carrier-phase measurements in comparison to the other two devices under test. However, it is also important to analyze the ambiguity nature of carrier-phase measurements from the device 3. Double difference carrier-phase measurements in a zero-baseline configuration must show an integer nature (within at least a quarter of a cycle) to be fixed correctly. The experimental setup shown in Figure 6 was therefore used to analyze the zero-baseline carrier-phase double differences of device 3. The Smartphone in this setup is placed near to the re-transmitting helix antenna (with amplified signal strength) to ensure no direct signal from the satellite is received within the Smartphone.



Figure 5: Code and Carrier Analysis with different Smartphones

Smartphone	Code Residual (m)	Carrier Residual (m)
Device 1	4.19	0.005
Device 2	3.95	0.003
Device 3	2.63	0.005





Figure 6: Zero-Baseline Retransmission Setup sketch for Carrier-Phase Double Difference Analysis

As can be seen in Figure 7, the double differenced carrier-phase measurements from device 3 with multiple satellites indeed show this integer nature. The experiment was performed multiple times to ensure that behavior is consistent. However, there were small jumps noticed due to the quantization error at the signal processing level Figure 7 (right) (Sharma et al. 2019). These jumps are found also for other satellites in the same epoch. They are small (1/10 of a cycle) in magnitude, and it is questionable if they do significantly impact the RTK solution up-to sub cm level. This experiment shows that under a good quality signal condition with low multipath and high SNR, the internal GNSS chip from the Smartphone (device 3) can provide continuous and good quality carrier-phase measurements.



Figure 7: Double Difference Carrier-phase (satellite G15 with highest elevation being the reference) with Zero baseline Retransmission setup for device 3 (Left), Quantization noise jumps in Double Difference Carrier-Phase (G15-G20)

2.3. Precise positioning Algorithms and Processing Tools (RTK/PPP)

To use the novel dual-frequency raw data output of the Smartphones, a highly configurable GNSS processing software is required. An analysis of available open-source processing tools showed that they were not able to adequately handle the poor quality of GNSS observations logged with Smartphones. Even in an open-sky conditions, the code noise of the Smartphone observations ranges from 2-3 m and can be significantly larger in multipath conditions. The open-source GNSS processing framework RTKLIB cannot readily use code pseudoranges with such high code noise as they might be flagged as outliers. The larger number of observations with high code noise makes the code measurements in-sufficient for SPP position and thus the majority of code and carrier-phase measurements get rejected before being processed with the RTK module (Sharma et al. 2018). Consequently, other processing options were investigated. A few of the available processing tools are presented in Table 4.

Processing Tools	Platform	Technique
MuSNAT (Licensed)(MuSNAT,2021)	Windows	RTK
Inertial Explorer (Licensed) (Inertial Explorer, 2021)	Windows	RTK/PPP
GNSMART (Licensed) (GNSMART, 2021)	Windows	RTK/PPP/PPP-RTK
RTKLIB (RTKLIB, 2013)	Windows	RTK
3PGo (Spaceopal et al. 2020)	Android	PPP
PPP-WizLite (PPP WizLite, 2018)	Android	PPP
GADIP3 (GADIP3, 2019)	Android	SPP/PPP + Logger
RTKDroid (RTKDroid, 2021)	Android	RTK

Table 4: List of Processing Tool

With commercially available processing tools such as Inertial Explorer (version 8.70.8722) or GNSMART the results were more adequate and ambiguity fixing was possible, provided sufficient quality of observation data was ensured through multipath suppression or retransmission.

2.4. Test Results - GNSS Only

Numerous studies show that the multipath effect poses a serious problem on precise positioning with the smartphone. Multipath mitigation methods to be potentially applied can be divided into three categories:

- 1) Before signal processing (through station selection and antenna design)
- 2) During signal processing (through receiver technology)
- 3) After the signal processing (through further processing of the observed variables)

None of the methods can eliminate the multipath effect completely and often a combination of the methods will give the best results.

The approaches related to receiver technology focus on advanced code measurements to suppress the effect of multipath. Due to the limited or no access to the IF samples, these techniques cannot be realized by the Smartphone app developer. On the other side, techniques for further pre-processing the observation data for multipath reduction are often based on averaging and are already implemented in the wide range of processing tools.

In the series of experiments presented in this Section, we considered the selection of the antenna environment as the easiest and most effective way to minimize the multipath effect. A very common and simple approach to reduce multipath is to optimize the antenna shielding, for example using a round ground plane. The optimal size as explained in (Scappuzzo et. al. 2009) is the 1.5 times wavelength of the operational frequency. However, the ground plane can only partially shield the multipath signals reflected from the floor. Due to the electrical conductivity of the material, the lower side of the ground plane can trigger surface waves on the upper side of the ground plane. These surface waves can overlap with the direct signal and reach the antenna. To reduce this effect, choke-ring antennas are used in applications where strong multipath reduction is required.

A simplified but instructive explanation of the effect of the choke-ring is the following: The reflected multipath signal hits the underside of the ground plane and generates a surface wave called primary wave as shown in Figure 8. This primary wave, when reflected from the bottom of one of the choke-ring, generates a secondary wave. Due to the ring depth of a quarter of the wavelength, the secondary waves when reflected have a phase shift of 180-degree w.r.t. the primary wave and hence attenuate the primary wave before it reaches the antenna element (Zhang Li. 2016).



Figure 8: Principal of Choke -ring Antenna (according to Filippov et. al 1998)

Static Measurements

To analyze the effect of choke-ring platform with Smartphone observations, the setup in Figure 9 (top) has been used. Two phones were placed on two geodetic pillars approx. 20 meters apart. One was placed on a choke-ring platform while the other was resting on a metallic ground plane. The coordinates of geodetic pillars are known within mm accuracy. A Trimble R10 integrated GNSS receiver/antenna was placed on another pillar and was used as a reference station. Starting from the raw GNSS data analysis, the quality of data collected with the device 3 (with choke-ring platform) is improved significantly when compared to the measurements of the phone without choke-ring platform. The sky plot below indicates that the identical satellites were recorded with both the Smartphones. However, the data quality analysis shows that the Smartphone with choke-ring platform has better observation data with less cycle slips (cf. Figure 9 bottom-right). Especially, for satellites with low elevation, device 3 without choke-ring shows a high amount of cycle slips.



Figure 9: Static Setup with choke-ring platform (left) and without choke-ring platform (right) (top) and Sky Plot (below). red vertical lines indicating cycle slip, yellow line indicate satellite with L1 frequency only, red line indicates satellites with L1/L5 frequency

To quantify the multipath suppression with the choke-ring platform, a multipath analysis was done with both the data sets. A significant improvement in the multipath was observed for the device 3 placed on the choke-ring platform (cf. Table 5).

Satellite-ID	Std. Multipath without Choke-ring [m]	Std. Multipath with Choke-ring [m]
G01	2.81	1.39
G22	2.11	1.62
G03	5.08	1.34
G17	4.22	2.81

Table 5: Multipath Analysis with Static Measurements

The RTK analysis was performed with Novatel Inertial Explorer using dual frequency GPS and Galileo observations data. The position analysis of GNSS observation data without choke-ring has mean error in the position w.r.t to true coordinates of pillar as 0.462 m, 0.0342 m and 2.921 m in x, y and z (ECEF- frame) respectively due to incorrectly fixed ambiguities. Whereas, with the choke-ring platform, the ambiguities

were fixed correctly and the mean error was reduced to 0.041 m, 0.032 m and 0.034m respectively (Figure 10) (Sharma et al. 2019).



Figure 10 : Positioning Results with choke-ring platform (left) without choke-ring platform (right)

With the success of the choke-ring experiments in both static and dynamic scenarios (Sharma et. al InsideGNSS 2019), an accuracy of the positioning solution is reached that is sufficient to localize the antenna phase center in the frame of the Smartphones.

Antenna Phase Center estimation

The phase center of the antenna is the (virtual) point where the signals transmitted from the satellites are collected. When a receiver reports a location fix, that location is essentially the phase center of the antenna. For a quality GNSS antenna, the electrical phase center will vary with the elevation or azimuth of the receiving signal by less than a few millimeters. However, with the Smartphone quality GNSS antenna, this variation is expected to be much higher as will be demonstrated later in this article.

A test setup was planned where the antenna phase center (APC) is estimated relative to the Smartphone geometry. The position accuracy of RTK-fix solutions in the (sub) centimeter range (Figure 12) and a precisely known position and orientation of the Smartphone in the same geodetic reference frame are considered together (Bochkati et at. 2019). A mounting frame with three attached Smartphones (device 3) was placed on a geodetic pillar. A Leica MS60 total station was placed on a neighboring pillar and used to determine the geometry of the Smartphones (see Figure 11).



Figure 11: Experiment setup for the exact determination of the Smartphone APC location, to be interpreted from top to bottom (Left), Experimental setup with real environment conditions for Smartphone APC determination (right)

Now the exact positions of the mounting frame were measured by means of the total station (Figure 11). Since the position of the center point of the support platform was known, namely that of the measuring pillar on which it is mounted together with the choke-ring, only the rotation relative to this center was missing in order to determine the absolute location of the mounting frame and the phones. This rotation was determined with the help of corresponding points. The points in the support platform system are very precisely known and were measured in the Cartesian measuring system. The rotation angle was estimated using a simple 2D rotation without translation (the measured points are considered relative to the coordinate of the measuring pillar and thus relative to the center of the support platform).

As a reference antenna with a known position is always required for the RTK solution, a geodetic receiver with a geodetic antenna was installed on another measuring pillar. The baseline between the measuring pillars is approx. 18 meters. Due to the short baseline, fixing of the ambiguities was fast and thus the position converged quickly. Both the raw measurement data from the reference station and from the Smartphones were processed in post-processing. The software package Inertial Explorer (version 8.70.8722) from Novatel was used for this purpose.



Figure 12: Sketch of the experiment setup depicted in the UTM32 global frame, north-oriented and the pillar reference coordinates have been subtracted from the output (Table 6)

Figure 12 and Table 6 show the results of this experiment. The positions of the fixed RTK solutions relative to the body of the phones show discrepancies among the three phones. While this is a first indication that antenna phase center (APC) might vary considerably between two phones of the same model, further investigations are necessary to rule out other influences as e.g. the satellite constellation during the measurement or interactions between the closely spaced phones. A full phase center variation (PCV) calibration for a Smartphone as described in the next Section can support such an analysis.

Smartphone	X[mm]	Y[mm]	2D-Error [mm]
Device 3 n1	-37.49	+63.30	30.43
Device 3 n2	-4.61	+139.63	18.88
Device 3 n3	+17.88	+58.34	29.53

Table 6: APC accuracy for different Smartphones under test

3. Smartphone Antenna

Since the beginning of the research on exploiting Android-based GNSS raw measurements, the Smartphone GNSS antenna has been recognized as one of the main limitations. Cheap GNSS antennas in the Smartphones are subject to low gain and poor multipath suppression. Mobile devices utilize an omnidirectional linearly or elliptically polarized antenna due to the unknown orientation of the Smartphone in use. This type of antenna has advantages in terms of received signal strength and the number of received signals (Pathak et al. 2003), but also makes the antenna very sensitive to the multipath (MP) effects. The latter limitation is generally accepted since the design drivers of Smartphone antennas are mainly cost and signal availability and not the observation data quality. Furthermore, not only the antenna itself but also other components of the phone, like the screen of the device and other transmitting antenna (Wi-Fi, Bluetooth), affect the Smartphone antenna (Xiao et al. 2019), leading to the reception pattern irregularities.

3.1. Need for phase center variation (PCV) estimation

Multipath and the radiation pattern of the antenna are the main site-dependent error sources of GNSS observations. Previous research as well as the work presented in Section 2 shows that the Smartphonebased code measurements are much noisier than measurements obtained with a geodetic-grade device. As mentioned above, much of this noise is due to the multipath that strongly affects the observations. Less noisy code measurement is the prerequisite to exploit full potential of the carrier-phase measurements. As correct ambiguity resolution depends on both the code and the phase measurement quality, it can be concluded that highly precise phase measurements are essential to solve ambiguities and achieve fast and precise Smartphone-based positioning.

in the Double – Difference analysis using short-baseline, the only differences between the two receivers are the site-dependent effects related to the type of antenna used and additional possible random biases. It has been shown that even in an optimal multipath environment, where no ground or wall reflections are possible (e.g., on the ground of a soccer field) some residual phase biases are visible. In this configuration, these residual phase biases are largely due to the radiation pattern of the antenna resulting in the so-called Phase Center Variations (PCV).

PCV refer to a mean center (the APC), an imaginary point thought of as the point where the signals are on average received. This center is typically not the Antenna Reference Point (ARP), which is a well-defined point accessible from outside the antenna. The mean phase center and the geometric offset to the ARP define the so-called Phase Center Offset (PCO), which is the vector between ARP and mean phase center, pointing towards the mean phase center. PCO and PCV are estimated by a specific procedure that is called antenna calibration.

3.2. Proposed Calibration Technique

Many research groups developed antenna calibration techniques, e.g., anechoic chamber measurements, relative and absolute field calibrations. The results presented in this article are obtained using the Geo++ absolute field robot-based calibration of GNSS antennas (Wübbena et al. 1997, Wübbena et al. 2000, Schmitz et al. 2002). Geo++'s approach has the following specific features:

• separation of PCV from multipath;

- absolute PCV, independent from any reference antenna;
- high accuracy and high resolution PCV;
- independent from station and location (e.g. multipath and geographic position);
- Field calibration method.

PCV can be expressed as a function of two angles, elevation, and azimuth, which gives the position of the source of the signal (i.e. the satellite). Spherical harmonics of degree eight and order five have been used to expand this function. The values of degree and order have been experimentally tested, showing that the obtained resolution was sufficient to model typical geodetic-grade antennas' disturbances while providing robust calibration results. Moreover, it is worth mentioning that the PCV is centered in order to have zero PCV values for zero values of the zenith angle.

3.3. Antenna calibration

Here, we report on the GNSS antenna calibration of the device 4 (Darugna et al. 2021). This device is equipped with a Broadcom BCM47755 chipset, which is a dual-frequency (L1/E1-L5/E5a) multi-GNSS receiver. Figure 1 depicts the setup for the Smartphone antenna calibration and the simplified dataflow to estimate PCO and PCV. The device 4 was mounted on the robot oriented upright, aligning the Smartphone geometrical center with the rotational center of the robot (corresponding to the ARP). The Smartphone's observations collected during the calibration have been post-processed in a multi-frequency GNSS antenna calibration along with GNSS observations from a geodetic reference station using an uncombined observation model. Eventually, PCO and PCV are written into an ANTEX format file w.r.t. Elevation and azimuth.



Figure 13: From left to right: robot antenna calibration setup and simplified processing scheme of the calibration of the Smartphone antenna. The device 4 was carefully mounted, allowing the device to be continuously charged. (Darugna et al. 2021)

The magnitude of the PCV is shown in Figure 14 and Figure 15 for L1 and L5, respectively. PCV magnitudes up to about 2 cm and 4 cm are observed, with formal STDs (1 σ) lower than 1.6 mm. These STDs are related to the variance-covariance matrix of the whole state estimation process. Consequently, they are affected by both the estimation of the parameters of the spherical harmonics and the quality of the observations. The device 4 PCV is larger than those of a typical rover antenna that typically shows PCV lower than 10

mm, with a smaller than 2 mm variation. The largest magnitudes of the PCV occur for azimuthal angles $\alpha \in [270^\circ, 360^\circ]$ for the L1 frequency (Figure 14) and for $\alpha \in [230^\circ, 360^\circ]$ for the L5 frequency (Figure 15).



Figure 14: L1 PCV of the device 4 Smartphone antenna. Polar and 3D plot with respect to azimuth and elevation are reported. (Darugna et al. 2021)



Figure 15: L5 PCV of the device 4 Smartphone antenna. Polar and 3D plot with respect to azimuth and elevation are reported. (Darugna et al. 2021)

In addition, distinct antenna phase centers have been estimated for L1 and L5, respectively. An analysis of the distribution of the PCV w.r.t. estimated antenna phase center showed that the largest absolute values of PCV are in directions of the major part of the Smartphone's body with respect to the phase center locations. The Smartphone components (housing and active electronics), as well as near field effects in that direction, might affect the signal reception resulting in larger PCV.

The repeatability of the antenna calibration has been assessed by performing twelve distinct antenna calibrations and comparing them w.r.t. a type mean. In the type mean correction, a rigorous adjustment of the individual PCV spherical harmonic expansions with their complete variance-covariance matrix is executed (Wübbena et al. 2006). A single antenna calibration duration goes from a minimum of six hours to a maximum of 37 hours. The elevation-dependency analysis shows that the agreement between the type mean and the individual calibration is better than 5 mm for elevations higher than 20°. For low elevations, significant discrepancies are visible for the azimuth angle ranges mentioned above. This is uncommon for the antenna calibration and may be attributed to the capability to calibrate the Smartphone antenna in those particular elevation and azimuth regions.

3.4. Limitations / Potential evolutions

The device 4 calibration shows estimated PCV that is much larger than expected for GNSS rover antennas. In addition, it seems that there is a lack of quality in the calibration for limited azimuth-elevation regions. This effect is more pronounced for the L5 frequency, compared to L1.

Different factors might contribute to the larger L5 PCV variation. Firstly, the tracking performance, in combination with the geometry of the constellation of L5-capable satellites, is not optimal (because not all the GPS satellites broadcast L5). Secondly, the device 4 is equipped with two distinct antennas for L1 and L5, and they might be of different quality.

However, considering the type of antenna, the repeatability of the calibration is considered good enough to apply the corrections in a positioning algorithm. The impact of such corrections is described in the next Section.

3.5. Impact of Antenna Calibration on positioning performance

In this experiment, the PCO and PCV corrections obtained from the calibration of device 4 (see Section 3.2) have been applied in the positioning algorithm of the Geo++ GNSMART software to perform Smartphone-based positioning. The PCO can be expressed in terms of PCV (Leick et al. 2015). Therefore hereafter, we refer to PCV as the total contribution. The concept behind the employed positioning algorithm is state space modeling (SSM). The main description of the SSM approach can be found in Wübbena and Willgalis (2001), and Wübbena et al. (2001). A local setup on the roof of the Geo++ building is considered. It is an open-sky environment, where several pillars with known coordinates present favorable locations for GNSS testing. The observations of a close (< 10 m) reference station have been exploited. For the tests, we assume that the two receivers experience the same atmospheric effects. The post-processing algorithm employs an extended Kalman filter (EKF) and an elevation mask of 10 degrees is applied. We achieved ambiguity fixed epochs with at least four satellites fixed to integers successfully. A satellite has been considered fixed when the ambiguity is fixed to an integer value for two frequencies (i.e., L1 and L5). The ratio test shows values higher than 3, being coherent with what is suggested by Euler and Schaffrin (1991).

Darugna et al. 2021 suggested that simple considerations about geometry and signal strength provide the user with a fast apriori indication about obtaining a precise solution with Smartphone's measurements based only on the geometry. 19 measurements with a good compromise between data quality and

satellite geometry were collected. It should be mention that for those experiment no choke ring multipath shielding was used.

Figure 16 shows the significant impact of the PCV corrections. While for all datasets only float solutions could be achieved without corrections, a centimeter-level fixed positioning was possible when applying them, it also indicates that the antenna corrections improve the float solution by roughly 1 cm. When applying the antenna corrections, a 2D RMSE of 1.6 cm and an RMSE of 3.8 cm in the height component can be achieved when the ambiguities are successfully fixed to integers. The time to fix ambiguities (TTFA) is less than 3 min in 84% of the cases, while all the 19 samples are fixed in less than 6 min, as shown in Figure 16 looking at the light blue colored lines. Moreover, a sub-meter 2D solution is obtained in about 1 minute. The relatively long time to reach sub-meter errors can be explained by the large code multipath error (Darugna et al. 2021). This leads to bad positioning performance during the first epochs, where the influence of the precise phase measurements is comparably small, and noisy code observations dominate the solution.



Figure 16: Positioning error RMS computed over 19 samples of data collected using the device 4 in a rooftop open-sky scenario. The application of antenna calibration corrections improves the positioning performance and allows ambiguity resolution, resulting in cm

As only a single Smartphone has been calibrated, no conclusion can be drawn regarding the apparent device-to-device discrepancies observed in Section 2.4. As an individual calibration of every Smartphone is certainly not feasible, it is an important next step to see whether a meaningful calibration can be produced that is valid for all phones of a certain model. Furthermore, the combined application of PCV corrections and multipath shielding with a choke ring might further improve the RTK performance.

4. Inertial Aiding

4.1. Need for Inertial Aiding

To obtain the full navigation information in mass-market consumer device such as Smartphones, i.e., 3D-position, -velocity and orientation, inertial aiding of the GNSS receiver is beneficial. Therefore MEMS - IMUs nowadays belonging to the standard set-up in every Smartphone can be used.

Many GNSS/INS integration methods have been developed to exploit the MEMS-IMU potential to improve the positioning performance for both indoor and outdoor applications. However, due to the inherent errors, e.g., higher noise level, temperature and vibration sensitivity, the benefit from the MEMS-IMUs is still limited. At this level, this sensor can be integrated with the dual-frequency GNSS observation, i.e., code-phase and carrier-phase to exploit the benefit of INS/GNSS-coupling, especially the tightly coupling version, where a reliable satellite measurement can provide a feedback to the IMU signal to calibrate its bias and scale factor error. In return, the error compensated IMU observations can support the GNSS receiver during short satellite outages, duty cycle gaps or high multipath scenario to propagate the navigation state with less accuracy degradation. The IMU could also contribute to the detection of cycle slips and ambiguity resolution. Despite all these advantages that the MEMS-IMU can deliver to improve the continuity and the stability of the positioning, very tedious calibration, such as 3-axis rotation table and climate chamber, and (stochastic) modelling procedures are needed to consider all error comports in the estimator filter (e.g., Kalman-Filter). Nevertheless, the accuracy of the sensor itself will not be changed, since the low-cost mass-market MEMS devices have a physical limitation that cannot be exceeded.

Glimpsing into the far future we note that a recently introduced micro gyroscope sensor (5mm diameter) based on fused-silica precision shell integrating (PSI) principle (wineglass gyro) with 0.0062°/Vhr ARW and 0.027 °/hr is at least 1000 times more sensitive than a conventional MEMS (Singh et al. 2020). These noise characteristics allows these devices to be categorized as (near) navigation grade IMU. Unfortunately, this technology is still in the prototyping phase in the laboratories and have not yet entered the mass market manufacturing. However, if they were widely adopted, they would definitively revolutionize the Smartphone's dead reckoning capability.

4.2. Smartphone IMU – quality check

In the last decades, the amount of Smartphone devices and types has been growing explosively. But the market of the MEMS-IMUs built in every Smartphone is still dominated by some big players in the field of MEMS-Fabrication dedicated for mass-market applications (for instance *TDK-Invensense, STMicroelectronics* or *Bosch Sensortec*). So, it is possible that different Smartphone manufacturers employ the same MEMS-chip, as can be seen in Table 7. Sometimes, (Staacks, et al., 2018) they also change the chip supplier company from one Smartphone generation to the next. In Table 7, some performance specifications (constant bias and Angle/Velocity Random Walk (ARW/VRW)) of different MEMS-Chips incorporated in recently introduced dual-frequency Smartphones are summarized. Some of them can be found in the smartphones ((Bochkati et al. 2019), (Darugna et al. 2021), (Wanninger.et.al. 2020) that have been used in the other research work. According to the manufacturer specifications, the quality of the TDK Invensense sensors seems to be better in terms of constant and stochastic errors. Nevertheless, these

tiny differences should be investigated more thoroughly in conjunction with the dual-frequency GNSS data, to see if the TDK Invensense chips outperform the STMicroelectronics-chips in term of accuracy.

Smartphone	IMU-Chip	IMU- Manufacturer	Constant Bias	ARW/VRW
Device 3	ICM-20690	TDK Invensense	Acc ~ $\pm 40 \text{ mg}$	Acc ~ 100 $\mu g/\sqrt{Hz}$
Device 5	-		Gyro ~ $\pm 1 \text{ deg/s}$	Gyro ~ 4 mdps/ $\sqrt{\text{Hz}}$
Device 6	LSM6DS3	STMicroelectronics	Gyro ~ ± 10 deg/s	Gyro ~ 7 mdps / $\sqrt{\text{Hz}}$
			$Acc \sim \pm 40 \text{ mg}$	Acc ~ 110 $\mu g/\sqrt{Hz}$
Device 7	ICM-42605	TDK Invensense	Gyro ~ ± 0.5 deg/s	Gyro ~ 3,8 mdps /√Hz
			$Acc \sim \pm 20 \text{ mg}$	Acc ~ 70 μ g/ \sqrt{Hz}
Device 4	LSM6DSM	STMicroelectronics	Gyro ~ $\pm 2 \text{ deg/s}$	Gyro ~ 3,8 mdps/√Hz
	_		Acc $\sim \pm 40 \text{ mg}$	Acc ~ 90 $\mu g/\sqrt{Hz}$
Device 8			e e	

 Table 7: Overview about the MEMS-IMU-chips integrated in some state-of-the-art dual-frequency Smartphones collected from the phyphox-App Sensor Database (Staacks, et al., 2018)

In Figure 17, the stochastic modelling of the ICM-20690 IMU-chip from three different dual-frequency Smartphones of the same model, namely the device 3, is shown. The assessment of the random processes available in both gyroscope and accelerometer signal is made by the mean Allan-Variance sequence. Additionally, for comparison, another commercial MEMS-IMU (XSENS MTiG-710) from the company "Xsens" is also shown.



Figure 17: Allan variance sequence for three different MEMS-IMU from device 3 compared to the commercial XSENS MTi-G-710 MEMS-IMU, gyro (left) and accelerometer (right)

According to the IEEE Standard Specification (IEEE Std 952-1997, 2018) we can see that the incorporated Smartphone accelerometer axes contain white noise (-1/2 slope), bias instability (flat region with 0 slope) and correlated noise (hill shape between cluster time = 1 s and 100 s). In comparison to the Xsens IMU, the axes of the device 3 accelerometer random processes are not identical, especially the z-axis which reflects the exact behavior of correlated noise that can be modeled as 1st-order Gauss-Markov (GM) process. Unexpectedly, all three Smartphones accelerometers show the same atypical behavior in the z-axis. This can be explained by the manufacturing process related to the MEMS-IMU technology. A three-axis MEMS accelerometer chip can sense accelerations as a reaction of the force applied to the chip

housing. The change in movement is equivalent to the change of capacitance between the moving structures of the chip. To guarantee the sensitivity in all three directions, i.e., x, y and z, two proof masses are available, namely a XY-axis proof mass and Z-axis proof mass that detect the in-plane and the out-of-plane accelerations respectively. But, due to the limited space in a Smartphone, the manufacturers usually tend to use a flat structure for the MEMS chip which results in different shapes for the XY and Z proof mass. On the other side, the Xsens-IMU exhibits a similar noise figure in all three-axes.

As depicted in Figure 17, the Allan variance diagram for the gyroscopes shows the same noise fluctuation for all axes and reveals at the same time, unexpected, less noise affecting the device 3-IMUs. Additionally, it can be seen, that both Angle Random Walk (ARW) and bias instability (BI) values of all three Smartphones gyros are smaller than those of the commercial Xsens device. For example, in the case of the device 3 gyro, the ARW parameters are smaller than 0,31 deg/h while the Xsens indicates amplitudes between 0,49 deg/h and 0,55 deg/h.

4.3. GNSS/INS Processing

The availability of the GNSS/IMU logger, paved the path for first trials of GNSS/INS combined processing. The GNSS data was logged with 1Hz, whereas the IMU data was logged using pre-defined rate constants "SENSOR_DELAY_FASTEST" provided by the Android system (approximately 300 Hz). The GNSS observation data can be logged in RINEX 3.03 format and IMU data is logged in ASCII format. It must be noted that for a successful GNSS/INS combined processing, both GNSS and IMU data should be synchronized to the same time scale. However, the GNSS data logged using GNSS/IMU logger is in GPS time and the IMU data is in the internal Android UNIX time that is synchronized to UTC via the mobile phone network. GNSS/IMU combined processing can therefore be performed without any dedicated synchronization mechanism (Guoyu et al. 2020), as the offset between GPS time and UTC time is known and can be applied. The synchronization accuracy might be limited and future update of the GNSS/IMU logger will consider use of Android internal counters.

In the first set of data logging, the Smartphone was held loosely in hand while riding the bicycle around a parking lot inside the UniBwM campus. The GNSS and IMU data was then passed to the loosely coupled GNSS/INS Kalman Filter implemented in MuSNAT. The MuSNAT Receiver was able to process SPP+IMU data as shown in MuSNAT Analyzer UI in Figure 18. The obtained attitude is correct, but the positioning results show room for further improvement.



Figure 18: MuSNAT Analyzer UI for SPP + IMU processing the brown dots are the GNSS/INS Filter output positions (left) Output Map View (right), Smartphone attitude from GNSS/INS integration filter (bottom)

To assess the performance of the Smartphone IMU in the context of GNSS/INS integration in a more focused way, in another experiment, two device 3 were fastened on the roof of a measurement van (see Figure 19). A high-end geodetic receiver (Trimble NetR9) and antenna (Trimble Zephyr 2) were fixed close to both devices to provide a reference trajectory. A commercial grade MEMS-IMU (Xsens MTi-G-710) was also mounted directly underneath to assess the quality of the TDK-Invensense IMU employed by the device 3. Furthermore, a local GNSS reference station located around 200 meters from the test track was running simultaneously to allow RTK-positioning. The trajectory environment contains both open-sky segments as well parts with buildings (elevation about 50 degrees) and dense foliage that can cause a significant signal attenuation and reflections. These parts, where a complete satellite signal blockage is present, are indicated in Figure 20 with the grey rectangles. In addition, an artificial GNSS data gap was introduced.



Figure 19: Measurement Van Setup (Bochkati et al. 2019)



Figure 20:Computed trajectory using different sensor combinations in ENU-frame; LC Trimble-Xsens (red), Trimble-M i8 (green) and GNSS-Only solution (blue). Observation gaps available in the GNSS-data are indicated with the grey rectangle (pink rectangle shows art



heading (left), pitch (center) and roll (right)

The recorded GNSS/IMU data were loosely coupled (LC) in different combinations, using the GNSS/INS post-processing software Inertial Explorer. Considering the Trimble NetR9-Xsens trajectory as reference, we can see that the device 3 IMU has a good performance, especially in term of the estimated attitude angles, i.e., heading, roll and pitch (Figure 21). At the beginning of the trajectory, the kinematic alignment delivers slightly different roll and pitch angles between the Xsens and the device 3 which is around 1 deg. This can be explained by the different noise standard deviation of the accelerometer axes, as depicted in Figure 17. The estimated heading information using both IMUs with the Trimble receiver are very closed to each other. Even though after introducing an artificial gap of about 20 second (see pink rectangles in Figure 20 and Figure 21) both IMUs were able to propagate the navigation solution correctly.

Therefore, in this demonstration, the LC with the Smartphone MEMS-IMU not only increases the availability of the positioning solution, but a smoothing behavior can also be achieved, if the LC-Filter, i.e. GNSS- and IMU-observation, can be tuned properly.

5. Conclusion and Outlook

Despite the latest innovation in the past years in the domain of Smartphone GNSS carrier phase positioning, there are still key limiting factors which need to be addressed before full scale use of Smartphones in high precision applications. Based on the gained experience during the last 3 years, we

see that the availability of dual frequency GPS/Galileo observations definitely enables ambiguity fixing but works only under a controlled condition only or otherwise in a partly unreliable way. The mixture of frequent cycle slips, biases and high noise/multipath is still a challenge for the processing algorithms.

The analysis performed revealed that the extremely poor multipath suppression of a Smartphone antenna together with the high PCV is a major impediment for cm level accuracy. Precise localization of the antenna phase center within the Smartphone, better understanding of antenna parameters like gain pattern (i.e. directivity of the Smartphone GNSS antenna), the PCV and analysis of the impact of human body interaction on gain and PCV still need to be addressed. Antenna PCV corrections can be applied during moving operations taking care of the Smartphone's attitude by using the internal IMU. The requirements concerning the precision of the attitude are correlated with the PCV pattern itself. Nonhomogeneous antenna patterns with sudden peaks would require more precise knowledge of the attitude than antennas with homogeneous patterns. For the analyzed case, the minimum requirement for the attitude precision would be 5°, i.e., as large as the calibration azimuthal resolution. Even smallest carrier-phase biases at chip level should be absent for cm level positioning to not further stress the RTK error budget. The ability to track the carrier-phase continuously in the strong multipath (including fading) conditions seems to be one of the most difficult requirements for the Smartphone GNSS chip. Additionally, getting access to the correlator values for understanding multipath mitigation at signal processing level might open new perspectives for the development.

In contrast to the GNSS antenna, the smartphone internal IMU demonstrates a surprisingly good performance. We clearly see a need for elaborated IMU error models, but once they are obtained the IMU will precisely aid the navigation solution even without relying on a dedicated motion model. This may in future algorithms include cycle slip repair or bridging of data gaps due to GNSS chip duty cycling.

Current RTK or PPP processing software packages seem not optimized to process the poor quality of Smartphone raw measurements. Investigations on optimal pre-processing of the observation data and improved cycle slip handling could therefore be beneficial. IMU aid cycle slip detection and correction with a tightly coupling fusion strategy and the development of extended sensor calibration models for smartphones could also be addressed.

Smartphone	Nomenclature
HTC Nexus 9	Device 1
Samsung S8	Device 2
Xiaomi MI8	Device 3
Huawei Mate20X	Device 4
HUAWEI P30	Device 5
Xiaomi Mi 9	Device 6
Xiaomi Mi 9T Pro	Device 7
HUAWEI P40 Pro	Device 8

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